

1 次の方程式を解きなさい。

(1) $4x + y = 6x - 2y = 14$

(2) $3x + y = 2x - 2y = 16$

(3) $-3x + 5y = 5x + 4y + 56 = -16$

(4) $-3x + 5y = 4y - 8 = -5x + 45$

1 次の方程式を解きなさい。

(1) $4x + y = 6x - 2y = 14$

$$\begin{cases} 4x + y = 14 & \dots\dots \textcircled{1} \\ 6x - 2y = 14 & \dots\dots \textcircled{2} \end{cases}$$

①と②の連立方程式を解くと、

$$\begin{array}{r} \textcircled{1} \times 2 \quad 8x + 2y = 28 \\ \textcircled{2} \quad \quad +) 6x - 2y = 14 \\ \hline \quad \quad 14x = 42 \\ \quad \quad \quad x = 3 \end{array}$$

$x = 3$ を①に代入すると、

$$\begin{aligned} 4 \times 3 + y &= 14 \\ y &= 2 \end{aligned}$$

答 $\begin{cases} x = 3 \\ y = 2 \end{cases}$

(3) $-3x + 5y = 5x + 4y + 56 = -16$

$$\begin{cases} -3x + 5y = -16 & \dots\dots \textcircled{1} \\ 5x + 4y + 56 = -16 & \dots\dots \textcircled{2} \end{cases}$$

②の式を整理すると、

$$5x + 4y = -72 \quad \dots\dots \textcircled{3}$$

①と③の連立方程式を解くと、

$$\begin{array}{r} \textcircled{1} \times 5 \quad -15x + 25y = -80 \\ \textcircled{3} \times 3 \quad +) 15x + 12y = -216 \\ \hline \quad \quad 37y = -296 \\ \quad \quad \quad y = -8 \end{array}$$

$y = -8$ を①に代入すると、

$$\begin{aligned} -3x + 5 \times (-8) &= -16 \\ -3x &= 24 \end{aligned}$$

答 $\begin{cases} x = -8 \\ y = -8 \end{cases}$

(2) $3x + y = 2x - 2y = 16$

$$\begin{cases} 3x + y = 16 & \dots\dots \textcircled{1} \\ 2x - 2y = 16 & \dots\dots \textcircled{2} \end{cases}$$

①と②の連立方程式を解くと、

$$\begin{array}{r} \textcircled{1} \times 2 \quad 6x + 2y = 32 \\ \textcircled{2} \quad \quad +) 2x - 2y = 16 \\ \hline \quad \quad 8x = 48 \\ \quad \quad \quad x = 6 \end{array}$$

$x = 6$ を①に代入すると、

$$\begin{aligned} 3 \times 6 + y &= 16 \\ y &= -2 \end{aligned}$$

答 $\begin{cases} x = 6 \\ y = -2 \end{cases}$

(4) $-3x + 5y = 4y - 8 = -5x + 45$

$$\begin{cases} -3x + 5y = -5x + 45 & \dots\dots \textcircled{1} \\ 4y - 8 = -5x + 45 & \dots\dots \textcircled{2} \end{cases}$$

①と②の式を整理すると、

$$\begin{cases} 2x + 5y = 45 & \dots\dots \textcircled{3} \\ 5x + 4y = 53 & \dots\dots \textcircled{4} \end{cases}$$

③と④の連立方程式を解くと、

$$\begin{array}{r} \textcircled{3} \times 5 \quad 10x + 25y = 225 \\ \textcircled{4} \times 2 \quad -) 10x + 8y = 106 \\ \hline \quad \quad 17y = 119 \\ \quad \quad \quad y = 7 \end{array}$$

$y = 7$ を③に代入すると、

$$\begin{aligned} 2x + 5 \times 7 &= 45 \\ 2x &= 10 \end{aligned}$$

答 $\begin{cases} x = 5 \\ y = 7 \end{cases}$